

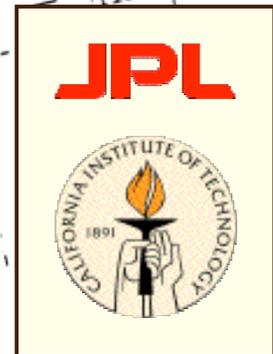
Goddard Space Flight Center  
November 18, 2004

**Synthetic LISA:**  
simulating the future  
of LISA data analysis

Tom Prince, Bonny Schumaker,  
Andrzej Królak, Jeff Edlund, Daniel  
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John Armstrong,  
Frank Estabrook,  
Massimo Tinto

Michele Vallisneri



# Tasting menu

- The LISA response: **geometric TDI**
- Simulating TDI: **Synthetic LISA** (w/Armstrong)

## Adventures in detector characterization with SynthLISA

- The effects of **noisy armlengths**
- **Post-processed TDI** (w/Shaddock, Ware, Spero)
- **TDI ranging** (w/Tinto, Armstrong)

## A quick survey of LISA sources: status and wishlist

- **Massive-BH** binaries
- **Extreme-mass ratio** inspirals
- The removal of **galactic binaries**
  
- A **conclusion** on simulation for LISA

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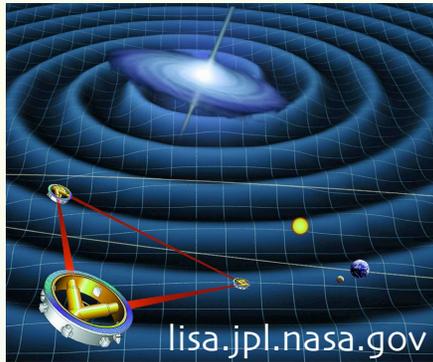
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# How is LISA an Interferometer?

LISA:



- A constellation of three **drag-free** spacecraft, separated by  $5 \times 10^6$  km and flying on an Earth-trailing solar orbit
- Gravitational waves detected in  $10^{-5}$ – $10^{-1}$  Hz band as modulation of distance between spacecraft by **picometer interferometry**
- Sources: **compact binary-star systems** in our galaxy, massive and super-massive **BH mergers**, compact stellar objects **captures** by massive BHs

Interferometer:

- (Noun) a **device that combines signals** radiating from a **common source** [*or multiple sources*], and received at **different locations** [*or at a common location, but after traveling different paths*]

TDI:

Armstrong+Estabrook+  
Tinto, Hellings, ...

- Six **laser beams** are exchanged between the spacecraft; each spacecraft **compares the phase** of the incoming and local lasers; these measurements are **delayed and combined** to synthesize interferometric observables

# The basic GW observable

In fact, with good clocks, any time transport link is a GW detector

$$h_{\mu\nu}^{\text{TT}} = h_+(t+x)[\mathbf{e}_{zz} - \mathbf{e}_{yy}] \leftarrow \text{plane GW prop. along } x$$

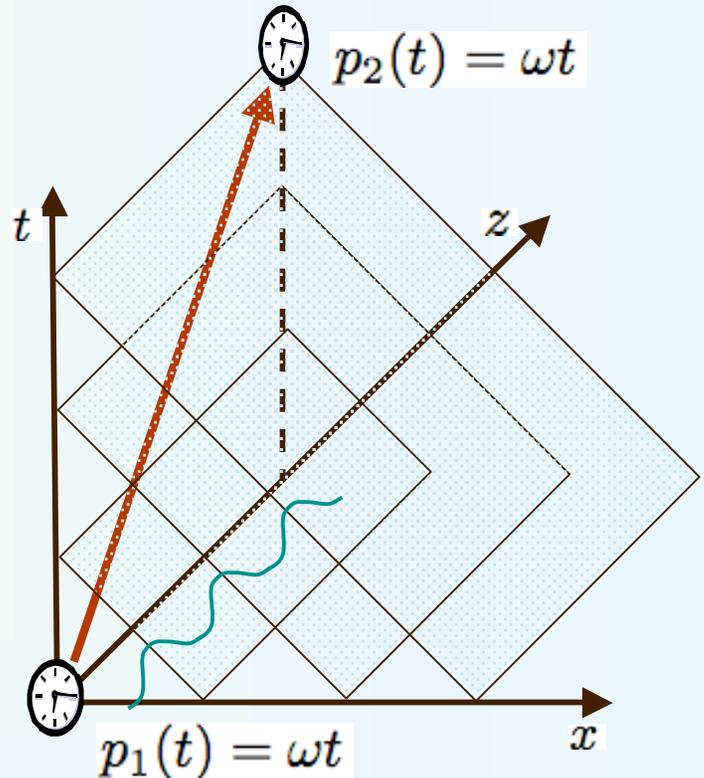
$$p_2(t) - p_1(t - L_{12}(t)) = \omega L_{12}(t)$$

$$L_{12}(t) = L_{12}^{\text{no gw}} + \frac{1}{2} \int_1^2 h_+(t) dt$$

$$[\dot{p}_2(t) - \dot{p}_1(t - L_{12}(t))]/\omega = \frac{1}{2}[h_+(2) - h_+(1)]$$

and in general  
(Estabrook-Wahlquist two-pulse response)

$$[\dot{p}_2(t) - \dot{p}_1(t - L_{12}(t))]/\omega = \frac{1}{2} \frac{\mathbf{n} \cdot [\mathbf{h}(2) - \mathbf{h}(1)] \cdot \mathbf{n}}{1 - \mathbf{k} \cdot \mathbf{n}} \leftarrow \begin{array}{l} \text{link dir. vector} \\ \text{wave propagation dir.} \end{array}$$

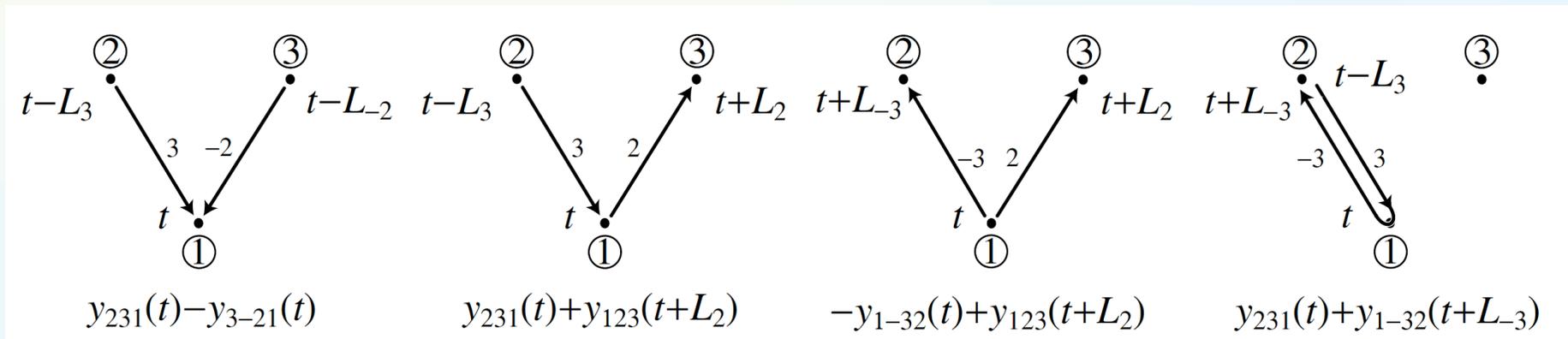


# Introducing TDI

But LISA's clocks (lasers) are not perfect: rms  $\Delta f/f = 10^{-13} \text{ Hz}^{-1/2}$   
 (160 dB louder than proof-mass noise)

$$\dot{p}_i(t) = \omega + C_i(t) + \text{g.w.}$$

Then we can add (or subtract) single-link observables  $y_{\text{send (link) recv}}$  to cancel laser noise at common events (with six LISA lasers, we will need also backplane measurements)

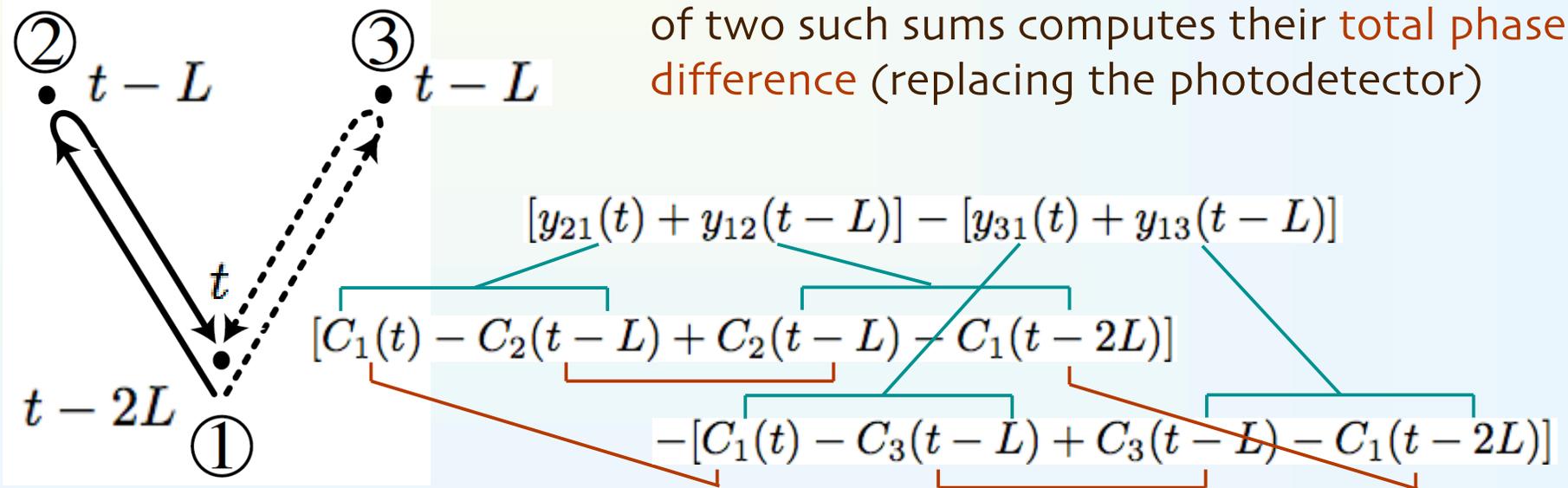


The geometric TDI principle: add/subtract single-link obs. to create a closed loop that cancels laser noise at all send/recv events

# Synthesized interferometers

The TDI combination of single-link observables can **synthesize the phase-difference output** of laser beams sent along standard interferometer paths:

- The **head-to-tail sum** of observables [e.g.,  $y_{12}(t) + y_{21}(t+L)$ , or  $y_{12}(t) + y_{23}(t+L)$ ] replaces a perfect **phase-locked transponder** (mirror)
- The **head-to-head or tail-to-tail difference** of two such sums computes their **total phase difference** (replacing the photodetector)

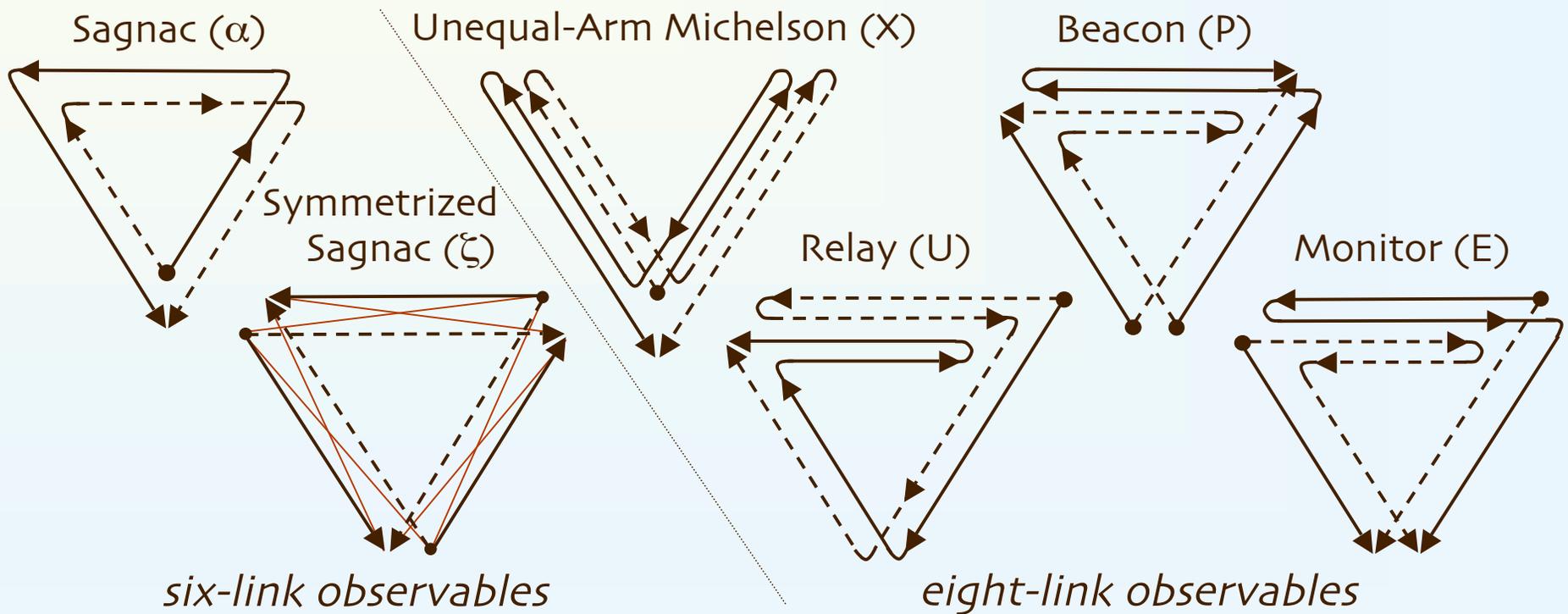


Synthesized equal-arm Michelson interferometer

# The garden of TDI observables

The **first-generation TDI observables**, discovered algebraically by AET:

- cancel laser noise in stationary unequal-arm LISA configurations
- are built with 6 single-link obs. (using all links), or 8 single-link obs. (using 4 out of 6 links); Dhurandar et al. (2002) give **generators**
- can all be interpreted geometrically as synthesized interferometers with 2, 4, or 6 beams!

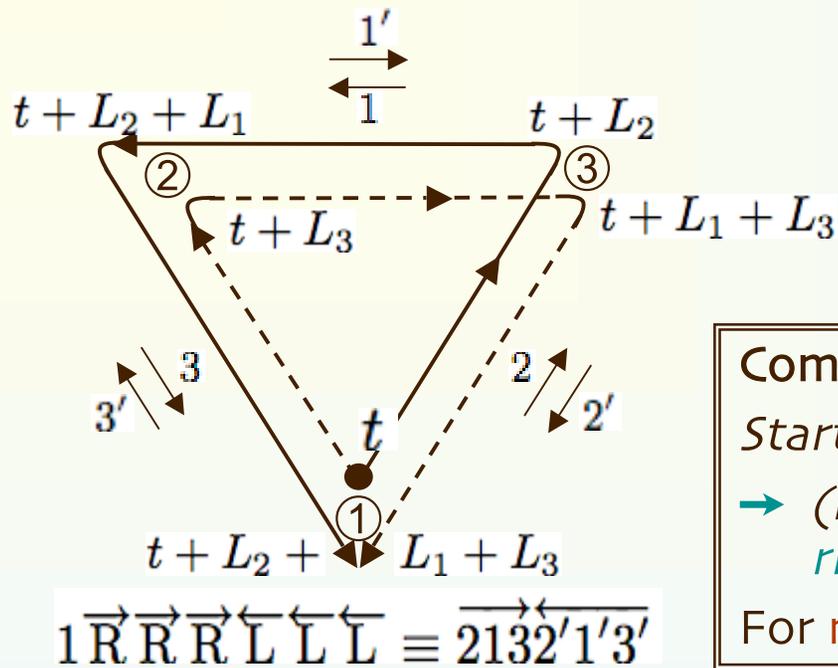


11/18/04

M. Vallisneri, Jet Propulsion  
Laboratory

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# TDI à la Feynman-Wheeler



The F-W TDI principle: a  $2N$ -beam combination can be seen as a single beam that travels forward and backward in time to meet itself back at its origin

**Combinatorial recipe for  $n$ -link combinations:**  
 Starting at arbitrary spacecraft, repeat  $n$  times:  
 → (randomly or exhaustively) choose left or right, choose future or past, lay down arrow  
 For  $n$  links,  $3 \times 2^{2n}$  combinations possible

**Closure rules to verify laser noise cancellation:**

- |L|-closure (first-generation TDI, unequal-arm LISA):**  
 $\#(1 \text{ or } 1'), \#(2 \text{ or } 2'), \#(3 \text{ or } 3')$  must be same under  $\rightarrow$  and  $\leftarrow$
- L-closure (modified TDI, rotating unequal-arm LISA):**  
 $\#(1), \#(1'), \#(2), \#(2'), \#(3), \#(3')$  must be same under  $\rightarrow$  and  $\leftarrow$
- L̄-closure (second generation TDI, flexing LISA; actual  $dL/dt=10^{-8}$  s/s):**  
 even more restrictive, will fit in a few lines of code

# Geometric TDI!

[MV, in preparation]

- Geometric TDI is a powerful (and pedagogical!) way to understand TDI
- It provides the first **systematic method** to **explore** the space of 2nd-gen. TDI observables. For instance:
  - the **shortest** 2nd-gen. obs. has length **16**
  - there is no **ξ-type** obs. up to (at least) length **20**
  - the search recovers TEA's **16-link, 2-beam**  $X_1, X_2, X_3$  but also news **4-beam** and **6-beam X-type** obs.
- The new combinations have the same sensitivity, but employ both time **delays and advancements**, with **reduced temporal footprint**

$$\begin{array}{c} \overrightarrow{22'3'33'322'} \overleftarrow{33'2'22'233'} \\ \overrightarrow{22'3'322'} \overleftarrow{33'2'2'3'3'2'233'} \\ \overrightarrow{3'322'} \overleftarrow{33'} \overrightarrow{22'} \overleftarrow{33'} \overrightarrow{22'3'3'2'22'22'2} \end{array}$$

links	combination space	unique observables	X	P,E	U	$\alpha$	2 beam	4	6	8
16	$4 \times 10^9$	45	9	18	18	0	3	24	0	18
18	$7 \times 10^{10}$	168	0	12	12	144	6	24	90	48
20	$1 \times 10^{12}$	618	24	12	18	564	12	114	264	84
24	$3 \times 10^{14}$ (4% done)	6,534 (160,000?)	29	24	40	6,440	48	536	1,540	...

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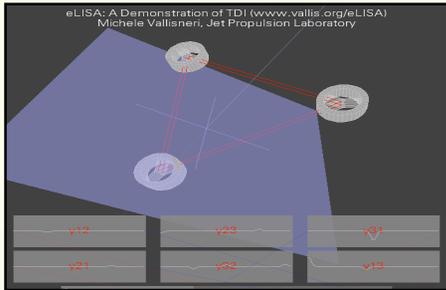
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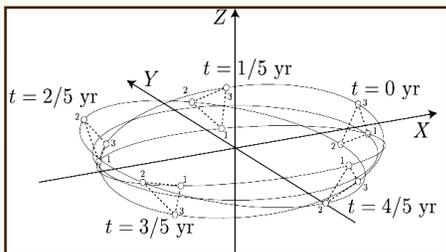
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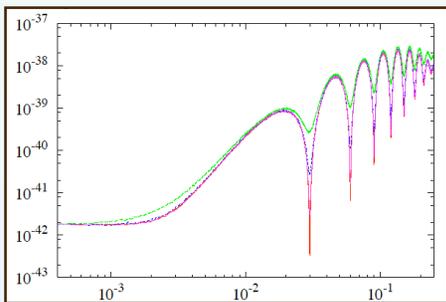
# Why simulate TDI?



The time-delay structure of the TDI observables generates complicated **many-pulse responses** to GW signals, making for **burdensome analytical signal models**



The LISA orbital motion **modulates GW signals**:  
→ by changing the orientation of the **LISA plane**  
→ by **Doppler shifting** incoming signals



The successful **subtraction of laser phase noise** must be verified w.r.t. the practical implementation of TDI and the realistic **time dependence** of the armlengths

# → Synthetic LISA

[by MV & J. W. Armstrong; MV, PRD, in review, gr-qc/0407102]

- Simulates the LISA fundamental noises and GW response at the level of science/technical requirements; can be adapted and extended to the analysis of systems-engineering questions
- Includes a full model of the LISA science process (shearing LISA motion, causal light propagation, second-generation TDI, laser-noise subtraction, phase locking)
- Contains standard noise and GW-signal objects, but it's easy to implement or load new ones
- Is conceived as a modular and steerable package, to allow easy interfacing to extended modeling and data-analysis applications
- Is user-friendly, and extensible (C++, Python, XML), to allow easy interfacing to extended modeling and data-analysis applications
- Is award-winning (NASA Space Act) software, (to be) released in the public domain

# A Synthetic LISA Block Diagram

**GW sources**  
for plane waves, work  
from  $k$ ,  $h_+(t)$ ,  $h_x(t)$  at SSB

**LISA noises**  
laser freq. fluctuations,  
proof mass, optical path

**LISA geometry**  
spacecraft positions  
→ photon propagation  
→ armlengths

**Doppler  $y_{ij}$**   
inter-spacecraft relative  
frequency fluctuations

**Doppler  $z_{ij}$**   
intra-spacecraft relative  
frequency fluctuations

**TDI  
observables**  
time-delayed  
combinations of  $y_{ij}$  and  $z_{ij}$   
laser-noise and optical-  
bench-noise free  
3 independent observables

# → The Synthetic LISA Package

Implements the LISA science process as a collection of C++ classes

## Class LISA

Defines the LISA time-evolving geometry (positions of spacecraft, **armlengths**)

**OriginalLISA**: static configuration with **fixed** (arbitrary) armlengths

**ModifiedLISA**: stationary configuration, rotating with  $T=1\text{yr}$ ; **different cw and ccw** armlengths

**CircularRotating**: spacecraft on circular, inclined orbits; cw/ccw, time-evolving, **causal** armlengths

**EccentricInclined**: spacecraft on eccentric, inclined orbits; cw/ccw, time-evolving, **causal** armlengths

**NoisyLISA** (use with any LISA): adds white noise to armlengths used for TDI delays

...

## Class Wave

Defines the position and time evolution of a GW source

**SimpleBinary**: GW from a physical monochromatic binary

**SimpleMonochromatic**: simpler parametrization

**InterpolateMemory**: interpolate user provided buffers for  $h_+$ ,  $h_x$

...

## Class TDI(LISA, Wave)

Return time series of noise and GW TDI observables (builds causal  $y_{ij}$ 's; includes **first- and second-generation** observables)

**TDInoise**: **demonstrates laser-noise subtraction**

**TDIsignal**: **causal**, validated vs. *LISA Simulator*

**TDIfast**: **cached** for multiple sources (**Edlund**)

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Check the sensitivity of **alternate** ...  
**LISA configurations**

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...

## Class Wave

Demonstrate **laser-noise subtraction**

→ 1st-generation TDI

→ modified TDI

→ 2nd-generation TDI

→ degradation of subtraction for imperfect knowledge of arms

...

## Class TDI(LISA, Wave)

Return time series of noise and GW TDI observables (builds causal  $y_{ij}$ 's; includes **first- and second-generation** observables)

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# → The Synthetic LISA Package

Implements the LISA science process as a collection of C++ classes

## Class LISA

Defines the LISA time-evolving geometry

Produce synthetic time series to  
**test data-analysis algorithms**

(arbitrary) armlengths

**ModifiedLISA**: stationary configuration,  
rotating with  $T=1yr$ ; **different cw and ccw**  
armlengths

**CircularRotating**: spacecraft on circular,  
inclined orbits, cw/ccw, time-evolving,  
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# Running Synthetic LISA

Synthetic LISA is steered with simple Python scripts  
What can we do with ten lines of code?

Import SynthLISA library	<pre>1 from lisaswig import * 2 from lisautils import *</pre>
Create LISA geometry object	<pre>3 lisa = EccentricInclined(0.0, 0.0)</pre>
Create noise object	<pre>4 noise = TDInoise(lisa, 1.0, 2.5e-48,                     1.0, 1.8e-37, 1.0, 1.1e-26)</pre>
Create GW object	<pre>5 wave = SimpleBinary(1e-3, 0.0, 0.0,                        1e-20, 1.57, 0.0, 0.0)</pre>
Create TDI object	<pre>6 signal = TDIsignal(lisa, wave)</pre>
Get X noise and X signal	<pre>7 noiseX = getobsc(2**16, 1.0, noise.Xm) 8 signalX = getobsc(2**16, 1.0, signal.Xm)</pre>
Write spectra to disk	<pre>9 writearray('noise.txt', spect(noiseX, 1.0, 64)) 10 writearray('signal.txt', spect(signalX, 1.0))</pre>

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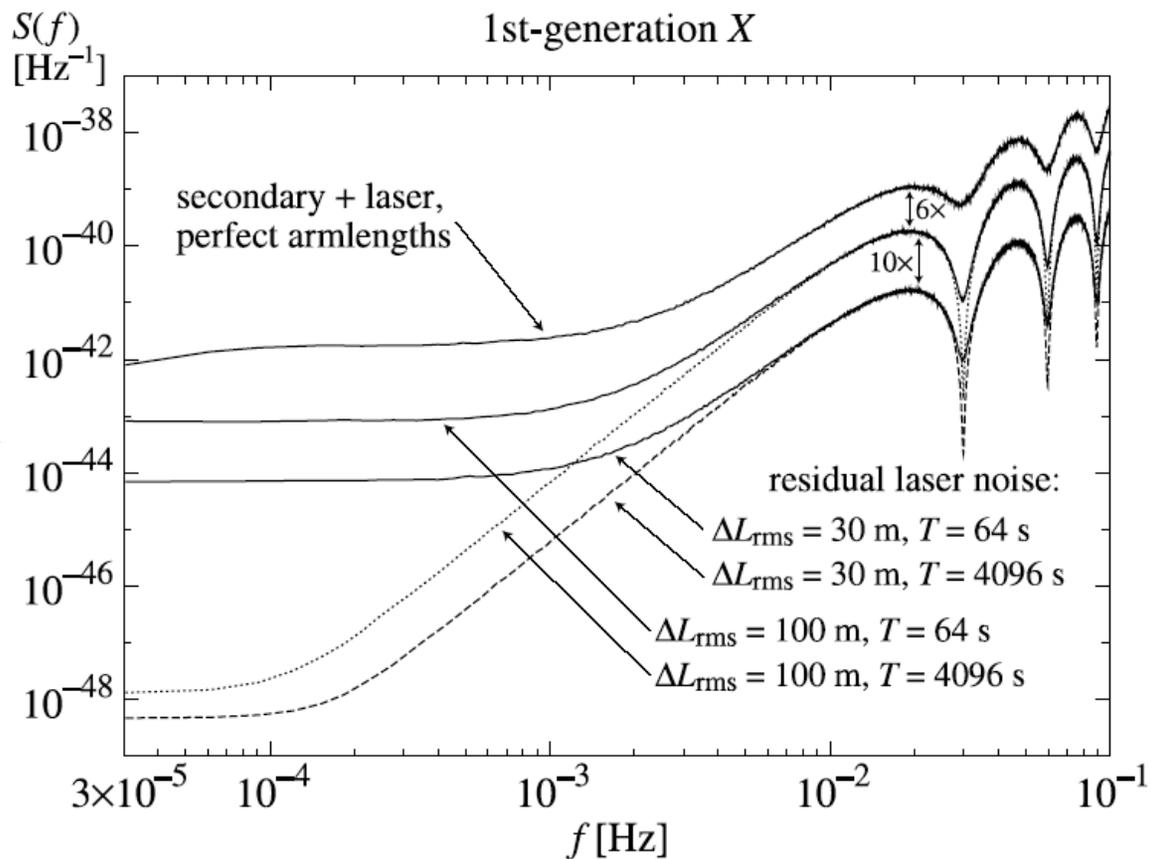
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# Case study: laser-noise cancellation for noisy armlengths

In accordance with analytical estimates, the **armlength-measurement tolerance** needed for first-generation TDI is  $\sim 50$  m, or  $1.7 \times 10^{-7}$  s (residual laser noise is still present because of flexing).

But much depends on the model of the armlengths used to assemble the TDI observables.

Using only **linear extrapolation** from the last two measurements...  
Paradoxically, it's bad to measure too often!



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# → Signal Interpolation for TDI!

[D. Shaddock, B. Ware, B. Spero, *MV, PRD 70, 081101(R) (2004)*]

Suppression of laser noise to 1 part in  $10^8$  with TDI requires armlength delays to be specified with a precision of 100 ns. How do we get phase measurements at the right times?

The current approach is to **trigger the phasemeters** at the TDI delays:

- Knowledge of the armlengths is needed on the spacecraft and in real time
- Spacecraft clocks must be **synchronized** to 100 ns
- Errors in armlength knowledge or synchronization lead to **irreversible corruption** of TDI combination

**Interpolation/post-processing** is the way:

- **Sample** phase measurements at (low) uniform rate; **transmit** the time series to Earth; **apply the TDI delays** by **interpolating** the time series; **Assemble** the TDI combinations in **postprocessing**
- Combining  $n \sim 20$  Lagrange interpolation with **oversampling** (10 Hz for 2.5 Hz-bandlimited phasemeter output), only 2 s of data needed to form observables
- **Ranging information** not needed in real time
- TDI implemented in postprocessing allows flexibility to choose **TDI schemes**
- Might require **higher data rates** (larger dynamical range)

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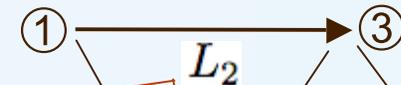
# → Time-Delay Interferometric Ranging

[M. Tinto, MV, J. W. Armstrong, gr-qc/0410122]

- As we said, the effective suppression of laser noise with TDI (to 1 part in  $10^8$ ) requires knowledge of the armlength delays to 100 ns
- The current LISA baseline assumes that a **dedicated** inter-spacecraft ranging subsystem will provide the armlengths with the required precision
- Enter **TDIR**: since laser noise cancels in the TDI combinations assembled with the correct armlengths, **find them** by **minimizing noise power** in the TDI combinations!
- From a similar idea by Gürsel and Tinto [1989]
- TDIR is **made possible** by **post-processed** (interpolated) TDI

$$X_1 = \left[ (y_{31} + y_{13;\hat{2}}) + (y_{21} + y_{12;\hat{3}'})_{;\hat{2}'\hat{2}} + (y_{21} + y_{12;\hat{3}'})_{;\hat{3}\hat{3}'\hat{2}'\hat{2}} + (y_{31} + y_{13;\hat{2}})_{;\hat{3}\hat{3}'\hat{3}\hat{3}'\hat{2}'\hat{2}} \right] + \dots$$

TDI-imposed delays: for good noise removal, must match the **physical propagation delays**



$$y_{31} = C_{13;2} - C_{31} + S_{31}$$

# A TDIR algorithm

→ Choose a TDI observable:

$$X_1 = \underbrace{X_1^{(0)}}_{\text{Laser noise}} + \underbrace{X_1^{(n)}}_{\text{Everything else}}$$

→ The minimum of the laser-noise-only  $X_1$  power gives the physical delays:

$$I^{(0)}(\hat{L}_k) = \frac{1}{T} \int_0^T [X_1^{(0)}(\hat{L}_k)]^2 dt$$

→ The presence of secondary noise (and GWs)...

$$I^{(n)}(\hat{L}_k) = \frac{1}{T} \int_0^T [X_1(\hat{L}_k)]^2 dt$$

Near the physical delays,  
sec. noise variations are  
negligible w.r.t. laser noise

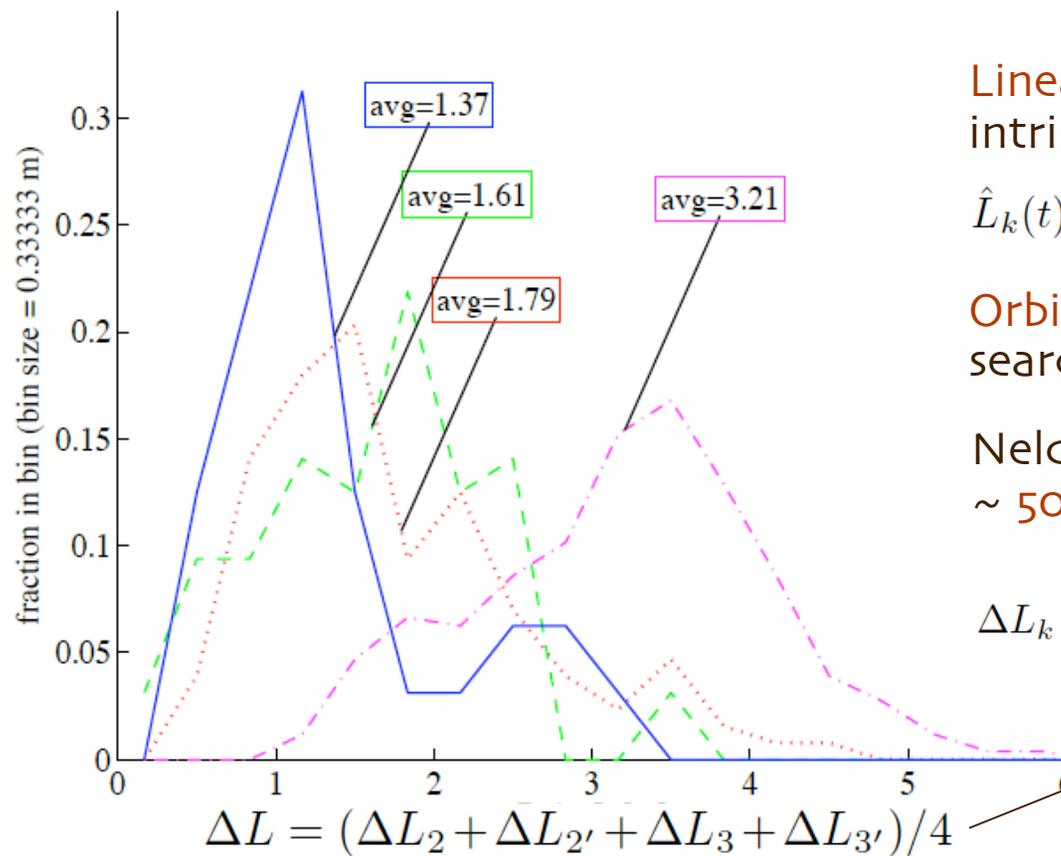
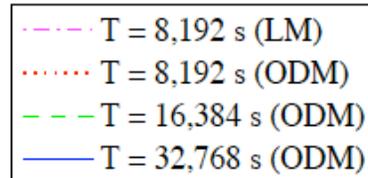
$$= I^{(0)}(\hat{L}_k) + \frac{1}{T} \int_0^T [X_1^{(n)}]^2 dt + \frac{2}{T} \int_0^T X_1^{(n)} X_1^{(0)}(\hat{L}_k) dt$$

...introduces an error  $\sim 30 \text{ ns} = 9 \text{ m}$  for  $T = 10,000 \text{ s}$

$$\delta L_k \sim \left( \frac{\sigma_{X_1^{(n)}}}{\sigma_{X_1^{(0)}}} \right) \sqrt{\rho/T}$$

rms power

# TDIR: simulation results



True armlengths:

$$L_k(t) = L + \frac{1}{32}(eL) \sin(3\Omega t - 3\xi_0) - \left[ \frac{15}{32}(eL) \pm (\Omega RL) \right] \sin(\Omega t - \delta_k)$$

Linear model (LM):

intrinsic error 0.25-2.60 m

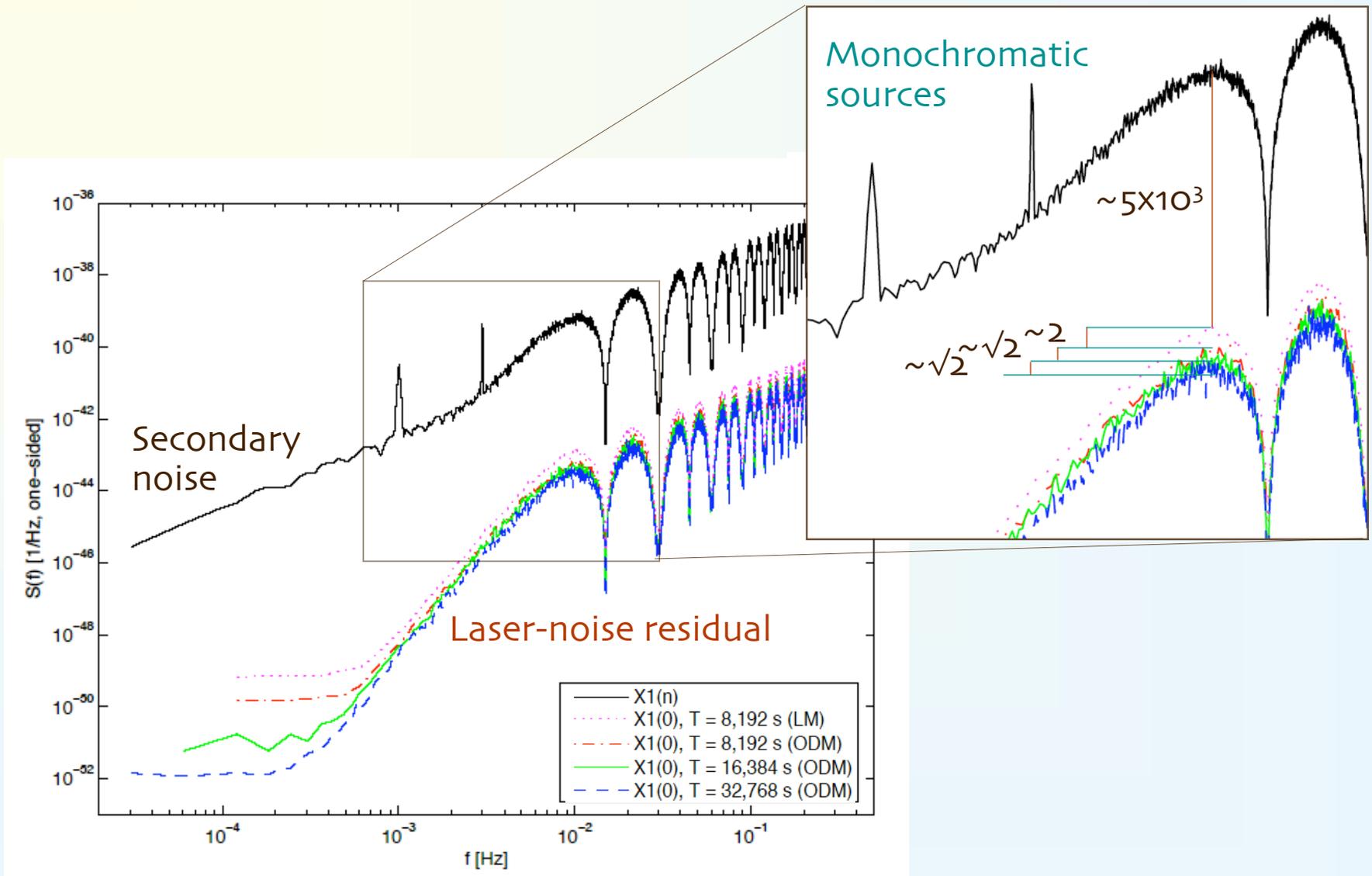
$$\hat{L}_k(t) = \hat{L}_k^0 + \hat{L}_k^1(t - t_0)$$

Orbital-dynamics model (ODM):  
search on  $eL, \Omega RL, \xi_0$

Nelder-Mead search, initial errors  
~ 50 km (Earth-based ranging)

$$\Delta L_k = \sqrt{\frac{1}{T} \int_{t_0}^{t_0+T} (\hat{L}_k(t) - L_k(t))^2 dt}$$

# TDIR: simulation results



## → TDIR: conclusions

- With  $T \sim 10,000$  s, TDIR allows the determination of the armlength delays with accuracy sufficient to suppress the laser noise  $\sim 10^3$  below the secondary noises
- The **error** induced in the reconstruction of **GWs** and **secondary noises** is

$$\begin{aligned} \sim dX_1^{(n)}/dt \times \delta L &= (2\pi f \delta L) \times X_1^{(n)} \\ &\sim 2 \times 10^{-8} X_1^{(n)} (f / 1 \text{ Hz}) (\delta L / 1 \text{ m}) \end{aligned}$$

- Although an **independent ranging** system will probably be included in the LISA design, TDIR provides **backup** and **fault tolerance**
- The armlength-delay determination can be **optimized** over the space of TDI observables
- TDIR is **conceptually distinct** from conventional one-way and two-way ranging: it employs a **phase-closure** relation between the measurements of three spacecraft
- Applicable in **other missions** that rely on **formation flying**?

# Tasting menu

- The LISA response: **geometric TDI**
- Simulating TDI: **Synthetic LISA** (w/Armstrong)

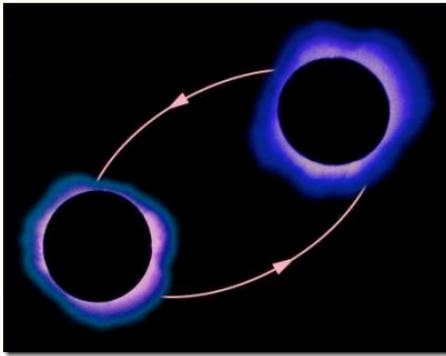
## Adventures in detector characterization with SynthLISA

- The effects of **noisy armlengths**
- **Post-processed TDI** (w/Shaddock, Ware, Spero)
- **TDI ranging** (w/Tinto, Armstrong)

## A quick survey of LISA sources: status and wishlist

- **Massive-BH** binaries
- **Extreme-mass ratio** inspirals
- The removal of **galactic binaries**
  
- A **conclusion** on simulation for LISA

# Black-hole binaries

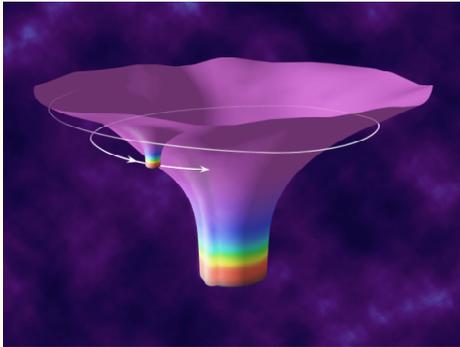


- Total mass  $10^3\text{--}10^6 M_{\odot}$ , detectable out to  $z \sim 5\text{--}10$
- In conjunction with EM detection, provide **standard candle** to measure equation of state of dark energy [Holz and Hughes, 2003]; accuracy limited by lensing
- If cosmological params well determined, study **galaxy-MBH coevolution** [Hughes, 2002]; “golden binaries” (insp.+ringdown) yield  $E_{\text{GW}}$  [Hughes and Menou, 2004]
- **Post-Newtonian inspiral** and **perturbative ringdown** well understood, at least for nonspinning binaries
- **Spin effects** in adiabatic inspiral: Buonanno, Chen, Pan, Vallisneri [PRD, 2004 (two papers)] developed a family of physical signal templates to search for **precessing, strongly spin-influenced** NS-BH and BH-BH inspirals

## Desiderata

- **Merger waveforms!** In the meantime: robust merger analysis algorithms [Brady and Majumdar 2004]; attention to reliability of waveforms [Miller 2003, 2004]
- Study **entanglement of spin and distance measurements** [MV+PBC, in progress]
- Study practicality of **coherent matched-filtering** detection: watch out for response modulation and confusion noise

# Extreme-mass-ratio inspirals

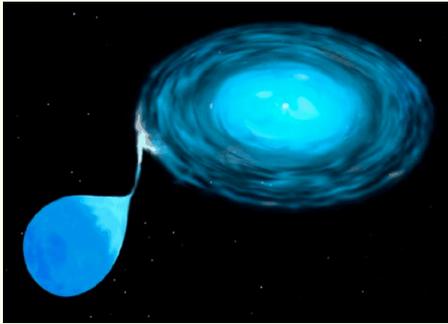


- Very complicated waveforms ( $10^5$  cycles/y, 14 params) to be computed using BH perturbation theory, and event rates exceedingly uncertain
- Very rich science payoff: map curvature of black-hole spacetimes, test no-hair theorems, get census of galactic cusp population
- Study of detection prospects [Gair et al. incl. MV, CQG 21 (2004)] :
  - assume matched filtering detection, evaluate CPU burden using kludge waves
  - coherent search not possible:  $>10^{13}$  templates for one month of integration
  - stacked search: eliminate phases, thread dynamical parameters through stacks
  - conclude  $\sim 1000$  detections/lifetime probable out to  $z = 1$

## Recent developments

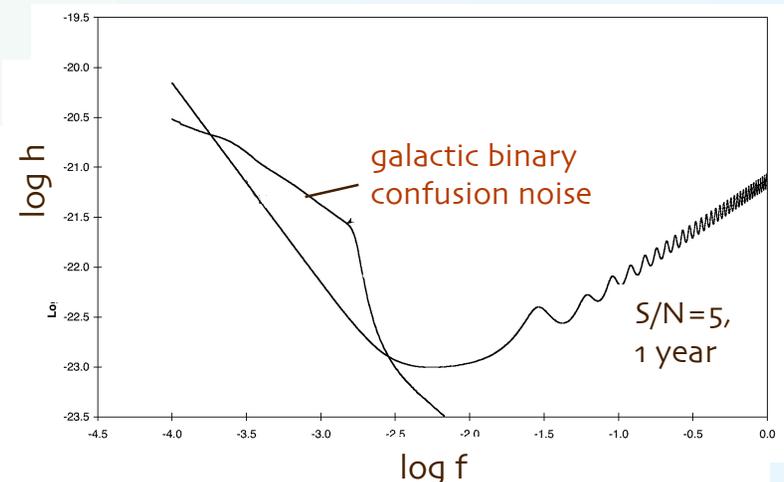
- Simpler TF power-excess detection for strongest events [Gair+Wen, in progress]
- IMBHs from runaway mergers in young stellar mass clusters [C. Miller, 2004]: IMBH-SMBH mergers (few/year?) visible without templates, test strong gravity
- Confusion noise from unresolved inspirals [Barack and Cutler, 2004]: weak to modest reduction of LISA sensitivity

# Galactic binaries



- Guaranteed **verification source**, but their ensemble generates confusion noise between  $10^{-4}$ – $10^{-2.5}$  Hz
- Low number of cycles/year: **when sources resolvable**, coherent detection possible
- **Analytical expression** of the TDI responses and ML detection scheme available [Królak, Tinto, and MV 2004]

- Rule of thumb: **confusion limit** at one binary/bin ( $f \sim 2 \times 10^{-3}$  Hz)
- gCLEAN [Larson and Cornish 2003]
- In practice: **parameter uncertainty** grows **exponentially** with # of binaries in bin; five-bin rule [Crowder and Cornish 2004]
- However: **directionality** of WD background [Seto and Cooray 2004, Tinto et al. 2004]



## Desiderata

- Problem of orthogonality (**baby/bathwater**) in background subtraction
- **Information-theoretical** understanding of LISA resolving power
- Maximum-entropy/Bayesian methods

# Tasting menu

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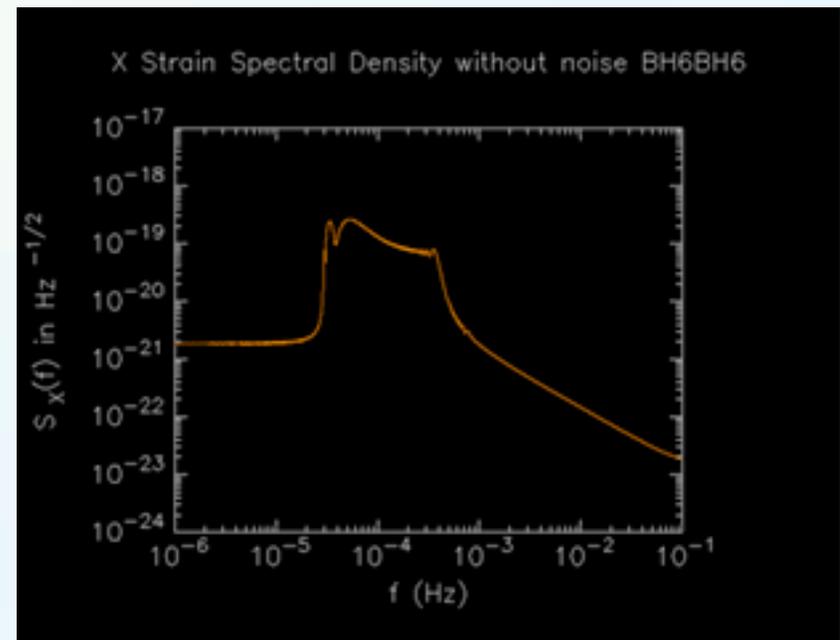
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# Mock LISA Data Archive



- Hosted at [astrogravs.nasa.gov](http://astrogravs.nasa.gov) (GSFC)
- **Steering Committee:** N. Cornish, J. Baker, M. Benacquista, J. Centrella, S. Hughes, S. Larson, M. Vallisneri
- Collect realistic time series of GW strains and of the LISA outputs, for use in developing and testing data-analysis algorithms

- Formulate **standard parameter conventions:**
  - **Where** is the source?
  - **Whence** the LISA orbits?
  - **Which** is the plus polarization?
  - **What** is X?
- As more contributions become available, will develop DB search and indexing capabilities
- Organize mock data challenges



# The Mock LISA Data Input Format

```
<?xml version="1.0"?>
<!DOCTYPE XSIL SYSTEM "xsil.dtd">

<XSIL Name="GWPlaneWaveSource">
  <Param Name="EclipticLatitude" Unit="Degree">40.0</Param>
  <Param Name="EclipticLongitude" Unit="Degree">180.0</Param>
  <Param Name="SourcePolarization" Unit="Degree">0.0</Param>

  <Time Name="StartTime" Type="ISO-8601">2004-07-15 06:30:00.0</Time>
  <Param Name="Cadence" Unit="s">1.0</Param>
  <Param Name="Duration" Unit="s">65536.0</Param>
```

- An application of XSIL (extensible scientific interchange language; also used as LIGO\_LW)
- Easily parsed by machine and human (web browsers, DBs)
- Inline or externally linked data
- Read/written by LISA Simulator and Synthetic LISA

Optional parameters go here

```
<Array Name="hp" Type="double">
  <Dim Name="Length">65536</Dim>
  <Dim Name="Records">1</Dim>

  <Stream Type="Remote"
    Encoding="Bigendian">
    hp.bin</Stream>
</Array>
</XSIL>
```

# Why simulations?

- The LISA response is **complex**
- **Honest** time-domain simulations can:
  - Take over where analytical treatments become unwieldy
  - Increase our trust in analytical insights
  - Point out the **unexpected**
- Uses of simulation:
  - Development and testing of **data-analysis** schemes and algorithms
  - **Performance** characterization and **architecture** tradeoffs
  - Interface between scientific and technical **mission requirements**
  - **Time-domain studies** of noise and vetos
- The future of simulation:
  - Waveform repositories (**astrogravs**), **data formats**, mock data challenges
  - Interface/incorporate **technical** simulations, experimental measurements
  - Requirement flowdown automation?
  - LISA stand in: prototyping of data-management system
  - Investigate other missions and geometries